

## 國立臺北科技大學 106 學年度碩士班招生考試

系所組別：1112 機械工程系機電整合碩士班甲組

## 第二節 自動控制 試題 (選考)

第一頁 共一頁

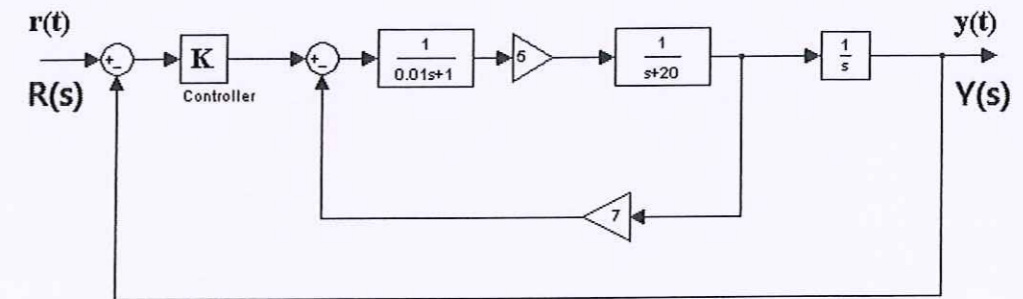
**注意事項：**

1. 本試題共 5 題，每題 20 分，共 100 分。
2. 請標明大題、子題編號作答，不必抄題。
3. 全部答案均須在答案卷之答案欄內作答，否則不予計分。

1. For a negative feedback system with loop transfer function  $GH(s) = \frac{10}{s(s+3)^2}$ 
  - (a) (5%) Find gain crossover frequency and phase margin.
  - (b) (5%) Find phase crossover frequency and gain margin.
  - (c) (5%) If a transportation lag  $e^{-Ts}$  is added to the loop (now the loop transfer function becomes  $GH(s)e^{-Ts}$ ), find the delay time  $T$  such that the system becomes marginally stable.
  - (d) (5%) If a gain  $K$  is added to the loop (now the loop transfer function becomes  $KGH(s)$ ), find  $K$  such that the system becomes marginally stable.
2. A unity-feedback control system with plant transfer function  $G_p(s) = \frac{1}{s(s+0.2)}$  is compensated by a Proportional-and-Derivative controller (PD controller with parameters  $K_p, K_d$ ), Please design the PD controller so that the closed-loop system have the following performances : (1) steady state error  $e_{ss} = 0.008$  when ramp input ( $r(t) = t$ ) is applied, (2) damping ratio  $\xi = 0.8$  for the closed-loop poles.
3. A characteristic equation  $F(s) = s^3 + s^2 + (K+2)s + 3K = 0$ , please plot the root locus for  $0 \leq K < \infty$ , and answer the following questions
  - (a) (4%) the starting locations and ending locations of the root loci.
  - (b) (4%) angles and centroid of the Asymptotes
  - (c) (4%) all the departure angles
  - (d) (4%) the intersection of the root loci with the imaginary axis; At the intersection, what is

- the corresponding value of  $K$ ?
- (e) (4%) the range of  $K$  such that the system is stable.

4. A dc motor is compensated by a proportional controller with gain  $K$ , as shown below.
- (a) (5%) Find the closed-loop transfer function  $\frac{Y(s)}{R(s)}$ .
  - (b) (5%) Find the range of  $K$  so that the closed-loop system is stable.
  - (c) (5%) Find the critical value of  $K$  so that the system is marginally stable. In such a case, the system will show oscillation when subject to a unit-step input, what is the oscillation frequency?
  - (d) (5%) If  $K=100$ , what is the steady state response of output  $y(t)$  when the reference input  $r(t)$  is a unit-step input function.



5. A system with transfer function  $\frac{Y(s)}{U(s)} = \frac{10}{(s+1)(s+2)(s+3)}$ , define state variables as  $x_1 = y, x_2 = \dot{y}, x_3 = \ddot{y}$
- (a) (8%) Find the state-space equation for the system.
  - (b) (12%) By use of the state feedback control law  $u = -\mathbf{K}\mathbf{X}$ , find the state feedback gain matrix  $\mathbf{K}$  so that the closed-loop system has poles at  $s = -1+2j, s = -1-2j, s = -10$ .