

ME04

# 國立臺北科技大學 108 學年度碩士班招生考試

系所組別：1112 機械工程系機電整合碩士班甲組

## 第二節 自動控制 試題 (選考)

第一頁 共一頁

### 注意事項：

1. 本試題共 5 題，每題 20 分，共 100 分。
2. 不必抄題，作答時請將試題題號及答案依照順序寫在答案卷上。
3. 全部答案均須在答案卷之答案欄內作答，否則不予計分。

1. A negative feedback closed loop system with loop transfer function  $GH(s) = \frac{K(s-1)}{s^4 + 2s^3 + 2s^2}$ ,

please plot the root locus for  $0 \leq K < \infty$ , and answer the following questions

- (a)(4%) the starting locations and ending locations of the root loci.
- (b)(4%) angles and centroid of the Asymptotes.
- (c)(4%) the intersection of the root loci with the imaginary axis; At the intersection, what is the corresponding value of K?
- (d)(4%) the departure angle of the complex conjugate roots (if any).
- (e)(4%) the range of K such that the system is stable.

2. A unity-feedback system with open-loop transfer function  $G(s) = \frac{K}{s(Js+2)}$ , the steady state error is 1 when subject to a unit ramp input; and the maximum overshoot is 0.2 when subject to unit step input, find K and J values.

3. A system with ordinary differential equation  $\ddot{y}(t) + 6\dot{y}(t) + 11y(t) = 2u(t)$  where y(t) is output and u(t) is input variable,

(a)(4%) find the transfer function of the system  $G(s) = \frac{Y(s)}{U(s)}$ .

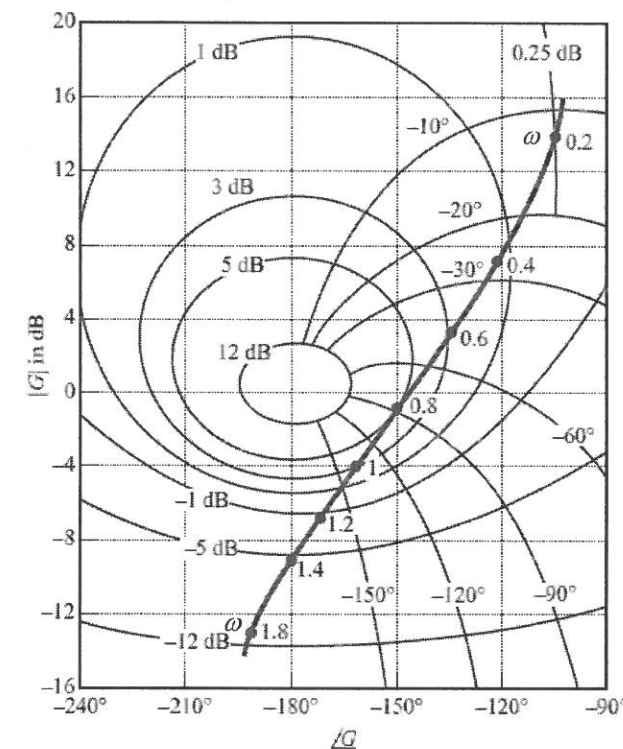
(b)(4%) find the poles and zeros of the system G(s).

(c)(4%) define state variables as  $x_1 = y, x_2 = \dot{y}, x_3 = \ddot{y}$ , find the state-space equation for the system.

(d)(8%) By use of the state feedback control law  $u = -\mathbf{KX}$ , find the state feedback gain matrix K so that the closed-loop system has a pair of dominant complex conjugate poles with undamped natural frequency  $2\sqrt{2}$  and damping ratio  $1/\sqrt{2}$  and an insignificant pole at  $s = -12$ .

4. A unity-feedback system with open-loop transfer function  $G(j\omega)$  locus shown in Nichols chart below,

- (a)(5%) please estimate (as best as you can) the gain margin, phase margin, gain crossover frequency, and phase crossover frequency.
- (b)(5%) Estimate the resonant peak, resonant frequency, and bandwidth.
- (c)(5%) If loop transfer function G(s) is multiplied by K, find the critical value of K such that the system becomes marginally stable.
- (d)(5%) If loop transfer function G(s) is multiplied by a transport lag  $e^{-Ts}$ , find the critical value of T such that the system becomes marginally stable.



5. A negative feedback closed loop system with loop transfer function  $GH(s) = \frac{2(T_2s+1)}{s^2(T_1s+1)}$ ,

Figures 1 and 2 are two Nyquist plots of GH(s).

- (a)(10%) For Figure 1, is it the case  $T_1 > T_2$  or  $T_1 < T_2$ ? and determine the closed loop stability using the Nyquist stability criterion.
- (b)(10%) For Figure 2, is it the case  $T_1 > T_2$  or  $T_1 < T_2$ ? and determine the closed loop stability using the Nyquist stability criterion.

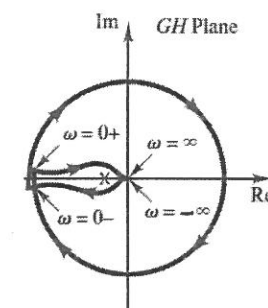


Figure 1

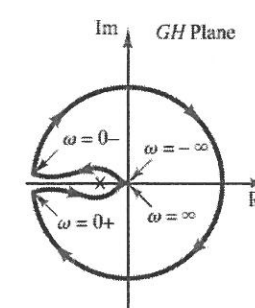


Figure 2