

# 國立臺北科技大學 110 學年度碩士班招生考試

系所組別：1502 自動化科技研究所

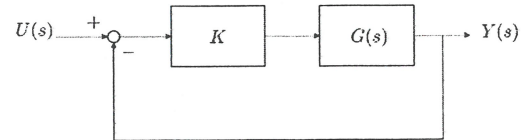
## 第二節 自動控制 試題 (選考)

第 1 頁 共 1 頁

### 注意事項：

1. 本試題共 4 題，共 100 分。
2. 不必抄題，作答時請將試題題號及答案依照順序寫在答案卷上。
3. 全部答案均須在答案卷之答案欄內作答，否則不予計分。

1. A closed-loop system with unity feedback has a transfer function  $T(s) = \frac{10(s+1)}{(s+1)^2 + 9}$ 
  - (a) Draw the Bode diagram for the **open-loop** transfer function  $G(s)$  roughly, including magnitude and phase vs frequency with semilog scale for the frequency axis. **(20%)**
  - (b) What is the gain margin? **(10%)**
2. Consider the transfer function  $G(s) = \frac{(100-s)}{(s+10)^2}$  with unity feedback. Please sketch the output response in time domain roughly. **(10%)**
3. Consider a closed-loop system shown in the figure



where  $G(s) = \frac{10(s+1)}{s(s-3)}$ .

- (a) What are the closed-loop poles and zeros? **(2%)**
  - (b) Sketch the root locus. **(15%)**
  - (c) Find the unit-step response  $Y(t)$ . **(5%)**
  - (d) Calculate  $Y(t)$  at  $0, 1, \infty$ . **(3%)**
4. The equation of motion for the simple pendulum is  $\ddot{\theta} + \omega^2 \theta = u$ .
    - (a) Please write the equation of motion in state space form. **(5%)**
    - (b) Design an observer (estimator) that reconstructs both states of pendulum given measurements  $\dot{\theta}$ . Assume  $\omega = 5 \text{ rad/s}$  and pick the observer roots to be at  $s = -10 \pm 10j$ . **(10%)**
    - (c) Write the transfer function of the observer between the measured value of  $\dot{\theta}$  and the estimated value of  $\theta$  (or  $\hat{\theta}$ ). **(10%)**
    - (d) Design the state feedback controller  $K$  so that the roots lie in  $s = -4 \pm 4j$ . **(10%)**