

國立臺北科技大學 100 學年度碩士班招生考試

系所組別：1201、1202、1203 製造科技研究所

第一節 微分方程 試題

第一頁 共一頁

注意事項：

1. 本試題共 6 大題，配分共 100 分。
2. 請標明大題、子題編號作答，不必抄題。
3. 全部答案均須在答案卷之答案欄內作答，否則不予計分。

1. Find the general solution of the following differential equation

$$\frac{dy}{dx} = \frac{y^2 - 1}{y(x^2 - x - 1)} \quad (16\%)$$

2. Find the general solution of the following Bernoulli equation.

$$y' - \frac{1}{x}y = x^3y^2 \quad (16\%)$$

3. Find the general solution of the following Euler equation $x^2y'' + 3xy' + 2y = 1$

(16%)

4. Solve the initial value problem : $y' - 3y = \delta(t - 1)$; $y(0) = 1$.

Where $\delta(t - a)$ is the Dirac delta function.

(16%)

5. Find the first three nonzero terms of the power series solution of the initial value problem, about the point where the initial conditions are given:

$$y'' - xy = 0, \quad y(0) = 1, y'(0) = 0.$$

(16%)

6. (1) Find the solution of the Sturm-Liouville problem:

$$y'' + \pi^2y = 0; y(0) = y(5) = 0 \quad (10\%)$$

- (2) Find the solution for the system of linear differential equations:

$$\begin{aligned} x_1' &= 5x_1 + 3x_2 & x_1(0) &= 0 \\ x_2' &= x_1 + 3x_2 & x_2(0) &= 4 \end{aligned} \quad (10\%)$$